REPORT DOCUMENTATION PAGE

Form Approved OMB No. 0704-0188

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1. REPORT DATE (DD-MM-YYYY)	2. REPORT TYPE	3. DATES COVERED (From - 10)
03-05-2011	Journal Article	
4. TITLE AND SUBTITLE		5a. CONTRACT NUMBER
Thermal Decomposition of 1,5-Dinit	robiuret (DNB): Direct Dynamics Trajectory	5b. GRANT NUMBER
Simulations and Statistical Modeling	g	5c. PROGRAM ELEMENT NUMBER
6. AUTHOR(S)		5d. PROJECT NUMBER
Jianbo Liu, Steven D. Chambreau, and	l Ghanshyam L. Vaghjiani	
		5f. WORK UNIT NUMBER
		23030423
7. PERFORMING ORGANIZATION NAME	(S) AND ADDRESS(ES)	8. PERFORMING ORGANIZATION REPORT NUMBER
AFRL/RZSP		
10 E. Saturn Blvd.		AFRL-RZ-ED-JA-2011-153
Edwards AFB, CA 93524-7680		
9. SPONSORING / MONITORING AGENC	Y NAME(S) AND ADDRESS(ES)	10. SPONSOR/MONITOR'S ACRONYM(S)
Air Force Research Laboratory (AFM	C)	
AFRL/RZS	,	11. SPONSOR/MONITOR'S
5 Pollux Drive		NUMBER(S)
Edwards AFB CA 93524-7048		AFRL-RZ-ED-JA-2011-153

12. DISTRIBUTION / AVAILABILITY STATEMENT

Approved for public release; distribution unlimited (PA #11140).

13. SUPPLEMENTARY NOTES

For publication in J. Phys. Chem. A.

14. ABSTRACT

A large set of quasi-classical, direct dynamics trajectory simulations were performed for decomposition of 1, 5-dinitrobiuret (DNB) over a temperature range from 4000 to 6000 K, aimed at providing insight into DNB decomposition mechanisms. The trajectories revealed various decomposition paths, and reproduced the products (including HNCO, N₂O, NO₂, NO, and water) observed in DNB pyrolysis experiments. Using trajectory results as a guide, structures of intermediate complexes and transition states that might be important for decomposition were determined using density function theory calculations. Rice-Ramsperger-Kassel-Marcus (RRKM) theory was then utilized to examine behaviors of the energized reactant and intermediates and to determine unimolecular rates for crossing the various transition states. According to RRKM predictions, the dominant initial decomposition path of energized DNB corresponds to elimination of HNNO₂H via a concerted mechanism where the molecular decomposition is accompanied with intra-molecular H-atom transfer from the central nitrogen to the terminal nitro oxygen. Other important paths correspond to elimination of NO₂ and H₂NNO₂₇. NO₂ elimination is a simple N-N bond scission process. Formation and elimination of nitramide is however dynamically complicated, requiring twisting a -NHNO₂ group out of the molecular plane, followed by an intramolecular reaction to form nitramide before its elimination. These two paths become significant at temperature above 1500 K, accounting for > 17% of DNB decomposition at 2000 K. This work demonstrates that quasi-classical trajectory simulations, in conjunction with electronic structure and RRKM calculations, are able to extract mechanisms, kinetics, dynamics and product branching ratios for the decomposition of complex energetic molecules, and predict how they vary with decomposition temperature.

15. SUBJECT TERMS

16. SECURITY CL	ASSIFICATION OF:		17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON
					Dr. Tommy W. Hawkins
a. REPORT	b. ABSTRACT	c. THIS PAGE			19b. TELEPHONE NUMBER
Unclassified	Unclassified	Unclassified	SAR	31	(include area code) N/A

Thermal Decomposition of 1, 5-Dinitrobiuret (DNB):

Direct Dynamics Trajectory Simulations and Statistical Modeling

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Abstract

A large set of quasi-classical, direct dynamics trajectory simulations were performed for decomposition of 1, 5-dinitrobiuret (DNB) over a temperature range from 4000 to 6000 K, aimed at providing insight into DNB decomposition mechanisms. The trajectories revealed various decomposition paths, and reproduced the products (including HNCO, N₂O, NO₂, NO, and water) observed in DNB pyrolysis experiments.

Using trajectory results as a guide, structures of intermediate complexes and transition states that might be important for decomposition were determined using density function theory calculations. Rice-Ramsperger-Kassel-Marcus (RRKM) theory was then utilized to examine behaviors of the energized reactant and intermediates and to determine unimolecular rates for crossing the various transition states.

According to RRKM predictions, the dominant initial decomposition path of energized DNB corresponds to elimination of HNNO₂H via a concerted mechanism where the molecular decomposition is accompanied with intra-molecular H-atom transfer from the central nitrogen to the terminal nitro oxygen. Other important paths correspond to elimination of NO₂ and H₂NNO₂. NO₂ elimination is a simple N-N bond scission process. Formation and elimination of nitramide is however dynamically complicated,

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requiring twisting a -NHNO $_2$ group out of the molecular plane, followed by an intramolecular reaction to form nitramide before its elimination. These two paths become significant at temperature above 1500 K, accounting for > 17% of DNB decomposition at 2000 K. This work demonstrates that quasi-classical trajectory simulations, in conjunction with electronic structure and RRKM calculations, are able to extract mechanisms, kinetics, dynamics and product branching ratios for the decomposition of complex energetic molecules, and predict how they vary with decomposition temperature.

I. Introduction

1, 5-dinitrobiuret (DNB, $C_2H_3N_5O_6$, molecular weight 193.08) is a very powerful and promising new explosive. 1-4 This nitrogen-rich compound was first synthesized by Thiele and Uhlfelder in 1898. 5 Recently, Klapötke and co-workers reported both experimental and theoretical studies of DNB, which determined DNB molecular structure, energetics, pyrolysis as well as detonation velocity and pressure. 1-3 DNB has an approximate planar structure, and the standard heat of formation ($\Delta_f H$) was calculated to be -353 kJ/mol (-1.829 kJ/kg) at the MP2/cc-pVTZ level of theory.² The enthalpy (Δ_rH) for the reaction of $DNB(s) \rightarrow 2CO_2(g) + 3/2 H_2O(1) + 1/4 O_2(g) + 5/2 N_2(g)$ was determined to be 1,003 \pm 39 kJ/mol $(5,195 \pm 200 \text{ kJ/kg})$ using bomb calorimetry.² DNB detonated strongly in the steel sleeve test, without the need of adding any additional oxidizer. The detonation velocity and detonation pressure were calculated to be 8.66 mm/µs and 33.9 GPa, respectively. ^{2,3} These values are close to those of the well-established energetic materials such as HMX⁶ (i.e. cyclotetramethylene-tetranitramine) and RDX⁶ (i.e. cyclotrimethylene-trinitramine). Thermal decomposition of DNB was examined by thermogravimetric analysis (TGA) and differential scanning calorimetry (DSC), and gaseous products were identified using mass spectrometry and Fourier transform infrared spectroscopy.^{1,4} DSC analysis revealed that thermal decomposition of DNB does not occur in a single step; instead it has several different activated reactions. The ultimate decomposition gases include HNCO, N₂O, CO₂, and water. However, the decomposition mechanism and dynamics have not yet been clearly established. One of the challenges is that the mechanisms involving highly reactive intermediates are difficult to probe experimentally, since such dissociation is a violent event and over within nanoseconds.

It is worth noting that Chambreau *et al.* reported a hypergolic ionic liquid fuel based on dicyanamide anions with white fuming nitric acid.⁷ Hypergolic systems are fuel-oxidizer combinations that ignite spontaneously upon mixing of two propellants at low temperatures and pressures, without the presence of an external ignition source. According to the proposed mechanism for the hypergolic ignition of dicyanamide anions with nitric acid, the reaction sequence results in the formation of DNB as an

intermediate in the ignition process.⁴ Therefore, a detailed understanding of mechanisms and dynamics of DNB decomposition is necessary for constructing an accurate kinetics model to predict the fuel performance, for optimizing the design of propulsion systems using hypergolic bipropellants, and for modifying and designing new fuels.

In the present study, thermal decomposition of DNB was probed theoretically. For complex molecules, especially for those with high internal energy content, use of chemical intuition to predict reaction pathways can prove unreliable. There may be concerted reactions that are difficult to predict, and once energy stored in the molecule begins to release, the system does not necessarily follow the minimum energy reaction path, i.e., the subsequent behavior is controlled by dynamics.⁸ Even for steps in the reaction that are controlled by statistical factors, standard transition state locating methods may be difficult to apply, because the molecular transformations are too complex. A useful approach to treating such system is quasi-classical, direct dynamics trajectory simulations, where the motion of the molecule is followed allowing the molecule to "show us" what the preferred reaction pathways are. The direct dynamics method dispenses with the potential energy surface. Instead, it calculates the energies, force constants, and Hessian "on the fly" using quantum chemistry methods. 9-17 This method becomes computationally attractive when the dimensionality of the system increases, particularly for the DNB molecule which contains 13 heavy atoms. Dynamics simulations partition the energy generated by exothermic reactions to vibrational, rotational and translational modes, increasing the chance of locating new reaction pathways. In addition, by following the variation of the potential energy during the trajectory rather than relying on intuition, we can identify better geometries for TS searching, as demonstrated below.

The remaining of the manuscript is organized as follows. Section II describes the methods of electronic structure/statistical calculations and quasi-classical trajectory simulations used to determine the thermal decomposition features of DNB. Trajectory simulation results are presented in section III, including an overview of the nature and time scales of trajectories we are simulating, the prescription for sorting trajectories, and contributions of various decomposition mechanisms at different temperatures.

Statistical modeling results are presented in section IV, starting with construction of the reaction coordinate for DNB decomposition using density function theory electronic structure calculations, proceeding to decomposition product branching using Rice-Ramsperger-Kassel-Marcus (RRKM) theory, ¹⁸ and finally to the analysis of inter-conversions of primary decomposition products. Conclusions are presented in section V.

II. Computational methodology

A. Electronic structure and RRKM calculations

To aid in reaction coordinate interpretation and get energetics information, density function theory (DFT) electronic structure calculations were performed at the B3LYP/6-31++G** level of theory, using the Gaussian 09 (B.01) suite of programs. Geometries were optimized by calculating force constants at every step. Vibrational frequencies and zero-point energies (ZPE) were scaled by a factor of 0.955 and 0.981, frequency corrected ZPE were added to the stationary point energies. All the transition states (TSs) found were verified to be first-order saddle points by frequency calculations, and the vibrational mode with the imaginary frequency to correspond to the reaction coordinate. When necessary intrinsic reaction coordinate (IRC) calculations were used to determine which minima are connected by a particular TS. To obtain more accurate energies of the reactant and products, calculations were also performed at the MP2/cc-pVDZ level of theory.

A transition-state-theory-based statistical model, Rice-Ramsperager-Kassel-Marcus (RRKM) theory, ¹⁸ was employed to examine the properties of the reactant, intermediate complex and transition states as a function of the total internal energy and associated angular momentum. The fundamental assumption in RRKM model is that energy is randomized and distributed statistically among all the energetically accessible states of the system, and the rate of a particular process (e.g., dissociation of a molecule, or inter-conversion between different isomers) is proportional to the total number of energetically accessible states at the transition state. ^{21,22} As a consequence, statistical reactions tend to occur by paths close to the minimum energy path, as the density of states is highest for such paths. ²³ RRKM unimolecular rates for crossing various transition states and density of states were calculated with

the program of Zhu and Hase,²⁴ using its direct count algorithm, and scaled frequencies and energetics from the DFT calculations. The angular momentum quantum number *J* used for RRKM calculations was determined from the corresponding DNB rotational energy, assuming DNB can be roughly treated as a nearly symmetric top molecule since two of the principle moments of inertia are not very different. Product branching is given by the ratio of the RRKM rates.

B. Quasi-classical direct dynamics trajectory simulations

In this study, direct dynamics trajectory simulations were conducted for two purposes: 1) investigating decomposition mechanisms of DNB at various temperatures, and discovering decomposition products;²⁵ and 2) locating key transition states for important decomposition paths, when the standard TSsearching methods (i.e., TS, QST2, and QST3 methods in Gaussian) fail. 26,27 Trajectory simulations started at the equilibrium geometry of DNB. A general chemical dynamics program VENUS of Hase et al. 28 was used to set up the trajectory initial conditions, and the Hessian-based method of Bakken et al. 17 implemented in Gaussian was used to propagate each trajectory with Hessians recalculated every five steps. The integrators were performed with a step size of ~ 0.4 fsec, which conserved the total energy to better than 10⁻⁴ Hartree. The SCF = XQC option was used during trajectory integration so that a quadratically convergent Hartree-Fock (OC-SCF) method ^{19,29} was adopted in case that the usual but much faster, first-order SCF method did not converge within the allotted number of cycles. Because millions of gradient and Hessian evaluations were required, the level of theory used for simulations was necessarily modest. To select a suitable level of theory, we calculated the enthalpy of combustion of DNB, 2 i.e., $\Delta_r H$ for $C_2H_3N_5O_6(s) \rightarrow 2CO_2(g) + 3/2 H_2O(l) + 1/4 O_2(g) + 5/2 N_2(g)$, using B3LYP and MP2 methods with 6-31G, 6-31G*, 6-31+G*, and 6-31++G** basis sets. The enthalpy of vaporization of water (44.00 kJ/mol) was taken from the NIST data base, ³⁰ and the enthalpy of sublimation of DNB was assumed to be close to that of biuret² (which is -126.7 kJ/mol from NIST³⁰). We then compared these results to the reported benchmark calculation at electron correlated MP2/cc-pVTZ level of theory,² and the results are listed in Table 1. It was found that the MP2 method ran into a convergence problem for DNB with the

selected basis sets. Compared to MP2/cc-pVTZ, all B3LYP methods underestimate $\Delta_r H$; however, including polarization in basis sets significantly improves the accuracy of DFT energetics. (Note that none of the calculated $\Delta_r H$ values, including the MP2/cc-pVTZ value, perfectly matches the experimental determined enthalpy of detonation of 1,003 kJ/mol, which is most likely due to uncertainty arising from the estimated enthalpy of DNB sublimation and different structures of DNB in the gas phase and in the crystalline state.²) On the basis of the overall level of agreement and computational speed, the B3LYP/6-31G* level of theory was chosen for the main set of trajectories. It is noted that the major purpose of our trajectory simulations is to probe the gross features of DNB decomposition, and to identify important decomposition paths.

The initial vibrational and rotational energies of DNB were sampled from Boltzmann distributions at specified temperatures. The quasi-classical initial vibrational states were simulated by giving each reactant atom displacement from equilibrium and momentum appropriate to the initial rovibrational state, with random phases for the different modes. The molecule has zero-point energy in all vibrational models. Because the decomposition time scale at typical detonation temperature would be far too long for practical trajectory simulations, simulations have to be carried out at high temperature. To identify a reasonable temperature range for dynamics simulations, we first ran a series of trajectories at a low level of theory HF/6-31G, at a temperature range of 1000 K to 8000 K. Within a trajectory simulation period of 4 psec, no dissociative trajectories were observed at temperature below 3000 K. At temperature of 3000 K, only 15% of total trajectories were dissociative. On the other hand, almost every trajectory underwent decomposition within a short time (< 0.4 psec) at temperatures higher than 6000 K. Therefore, three temperatures, 4000, 5000 and 6000 K, were chosen for running trajectory simulations at the B3LYP/6-31G* level of theory. For each temperature, batches of trajectories (50 trajectories each) were calculated. Trajectories were propagated for a preset length of time (~ 4 psec), or until the distance between the decomposition products exceeded 9.0 Å. A total of 150 trajectories were completed at the B3LYP/6-31G* level of theory in the course of the study reported here, each taking ~ 380 CPU hours on

an Intel Core 2 dual and Core 2 quad (3.0 GHz)-based 64 bit Linux computational cluster. Thus the complete set of trajectories required about 6.5 years of CPU time on the cluster. The program gOpenMol was used for trajectory visualization.³¹ Detailed analysis of individual trajectories and statistical analysis of the trajectory ensemble was done with programs specifically written for this purpose,^{27,32-37} available from the corresponding author upon request.

One issue with using quasi-classical trajectory methods is that vibrational energy is not quantized in molecules. Lack of quantization presumably has an effect on how energy is distributed between vibrational modes during trajectories and upon dissociation.^{38,39} It is possible to have trajectories where the product vibrational energy is below the zero point level. Such unphysical trajectories were found to be negligible in our trajectories, presumably because we are looking at relatively high internal energies (see Table 2), reducing the error associated with treating the motion classically.

As mentioned above, temperatures used for simulations are much higher than the detonation temperature, which was ~1500 K estimated from the temperature of the Bunsen burners used in experiments⁴⁰ (For reference, the experimentally measured DNB decomposition temperature is around 405 K).¹ Table 2 lists the estimated vibrational and rotational energies at various temperatures. As a result, some trajectories may find decomposition paths with barriers too high to be relevant to decomposition at realistic temperatures. The trajectory observables of greatest interest for our purpose are decomposition mechanisms. The point is that with enough trajectories, *all* important reaction paths will be found, including those that control decomposition under the conditions of interest. Once decomposition paths are identified, the corresponding reaction energetics including activation barriers can be calculated, and only those which are able to contribute need be included in decomposition kinetics modeling.

III. Trajectory Results

Before we discuss the quasi-classical trajectory simulation results, it is useful to review the nature and time scales of the trajectories we are simulating. Trajectories were run at the temperature range of 4000 to 6000 K. At the temperature of 4000 K, 10% of trajectories maintained the intact molecular structure

when trajectories were terminated at 4 psec. The remaining 90% of trajectories at 4000 K and all trajectories at 5000 and 6000 K underwent thermal decomposition via direct, concerted or sequential mechanisms before the termination of trajectories. For most of the decomposition trajectories, the time at which the DNB molecule begins decomposition is between 0.2 and 3 psec – longer than the periods of most DNB vibrational modes. The decomposition trajectories can be grouped into six classes as summarized in Table 3. Table 3 also compares their product energetics, and relative efficiencies at different temperatures. The structures of DNB and all decomposition products observed in trajectories are depicted in Figure 1. All these structures were optimized at the B3LYP/6-31++G** level of theory. Video files showing representative trajectories for each of six classes are provided in the supporting information.

A. Decomposition path 1 (production of isocyanic acid and NO₂)

By far the most common outcome of DNB trajectories is path 1, which accounts 34 - 43% of all trajectories at 4000 - 6000K. Path 1 starts with elimination of NO₂ from DNB, followed by consecutive elimination of two isocyanic acid (HNCO) molecules from the derivative intermediate. The endothermicity of NO₂ elimination is 1.73 eV, and that of subsequent elimination of two HNCO molecules is 2.43 eV, both of which were calculated with respect to the DNB molecule. Figure 2 demonstrates a trajectory (calculated at 4000 K) representative of path 1. The figure shows the change of potential energy (PE) during the trajectory. The oscillations in the PE reflect the vibration of the DNB molecule and the products, including ZPE. The time scale of decomposition depends on the simulation temperature, but three numbers are relevant. The time between trajectory starts and the onset of NO₂ elimination is around 150 fsec. The time for elimination of the first HNCO molecule from the remaining structure is around 410 fsec, and the time for elimination of the second HNCO is around 800 fsec. In addition to the multi-step elimination process indicated in Figure 2, a small fraction of path 1 trajectories (< 10%) experienced simultaneous elimination of NO₂ and HNCO.

B. Decomposition path 2 (production of HNNO₂H)

Another common class of decomposition trajectories belongs to path 2, accounting for 7 - 26% of all trajectories at 4000 - 6000K. In path 2, HNNO₂H is produced via intra-molecular hydrogen atom transfer followed by breaking an amide bond. HNNO₂H may further decompose to N₂O and water. While the first step is endothermic by 0.99 eV, the overall decomposition process, i.e., DNB \rightarrow O₂NNHCONCO + N₂O + water, is exothermic by 0.93 eV with respect to DNB. A trajectory representative of path 2 is illustrated in Figure 3, indicating the energy barriers associated with two activated decomposition steps of which the second one is much more significant. Note that in principle another pathway may produce the same products as path 2, i.e., DNB completely decomposes to O₂NNHCONHCO and HNNO₂, subsequently undergoes inter-molecular hydrogen atom transfer between two fragments to produce HNNO₂H. However, this decomposition route involves breaking a CN bond with an energy barrier in excess of 3.55 eV calculated at B3LYP/6-31++G**. Therefore, this decomposition path is less likely to contribute to a significant extent in typical detonation.

C. Decomposition path 3 (production of nitramide)

Path 3 contributes to 10% of all trajectories at 4000 K, and the contribution decreases at high temperatures (6% at 5000 K and 4% at 6000K). Figure 4 shows a typical trajectory for path 3. In this decomposition path, DNB rotates a –NHNO₂ unit out of the molecular plane, and then undergoes an intramolecular S_N*i*-reaction to form nitramide H₂NNO₂ by transferring a hydrogen atom from the central N atom to the neighboring amine N, followed by elimination of nitramide. This decomposition path has been proposed in the literature, ^{1,4} and the product nitramide was identified in the mass spectrum of DNB pyrolysis products. Similar to HNNO₂H, nitramide may also decompose to N₂O and water in the gas phase. ¹

D. Other decomposition paths

The remaining trajectories can be characterized as paths 4, 5, or 6, respectively. These paths are much less common, but they are similar in that all involve sequential decomposition reactions and the first step is NO₂ elimination. In path 4, an inter-molecular hydrogen atom transfer reaction occurs between two fragment compounds O₂NNHCONHCONH and NO₂, producing O₂NNHCONHNCO and nitrous acid

HONO. As visualized in path 4 trajectories, when the radical fragments O₂NNHCONHCONH and NO₂ (produced from a barrierless dissociation path, *vide infra*) separate ~3 Å, roaming reorientation becomes feasible and this leads to intermolecular H abstraction by NO₂ from O₂NNHCONHCONH, giving molecular product NO₂H with large vibrational excitation of the nascent O-H bond. This decomposition path is to some extent similar to a roaming radical reaction discovered recently.⁴¹ In some path 4 trajectories, nitrous acid inter-converts to HNO₂. At all temperatures, only 10% (or less) of all trajectories lead to path 4. In path 5, O₂NNHCONHCONH undergoes extensive dissociation to NO₂, isocyanic acid, and a three-membered ring intermediate cyclic-HNCONH. The relative efficiency of path 5 increases significantly at high simulation temperatures, i.e., 8% at 4000 K and increasing to 13% at 5000 K and 27% at 6000 K, presumably because this is the most endothermic reaction route. Finally, oxygen atom transfer between O₂NNHCONHCONH and NO₂ was observed in path 6, leading to net "NO elimination" from DNB. However, path 6 only occurs at 5000 K with an efficiency of 5%, and was not observed at 4000 and 6000 K.

These trajectory results lead us to predict that paths 1, 2 and 3 may represent typical decomposition pathways of DNB, particularly in the view of the initial decomposition steps. These paths are chosen for several considerations. First, paths 1, 2 and 3 are energetically more favorable and overall attained much higher probabilities than others in trajectory simulations. Second, the products identified in trajectories of paths 1-3, including HNCO, N₂O, NO₂ and water, were all observed experimentally.^{1,4} Therefore, these trajectories are in reasonable agreement with experiments, and can be used as a guide to extract additional mechanistic insight with confidence. On the other hand, NO (one of path 6 products) accounted for only small amount of pyrolysis products, and HNO₂ (one of path 4 products) was not observed in pyrolysis.¹ Therefore, contributions of paths 4 and 6 are expected to be negligible. Path 5, regardless of any possible energy barriers, has an endothermicity of 3.02 eV and is therefore of less importance as well.

The following electronic structure calculations and statistical analysis focus on the initial decomposition steps of DNB, i.e., elimination of NO₂, HNNO₂ and H₂NNO₂. It is worth noting that paths 4, 5 and 6 are all related to path 1 in that these paths share a common rate-limiting step, i.e., NO₂

elimination. Consequently, all possible decomposition paths identified in trajectory simulations are included in the present statistical modeling.

IV. RRKM Modeling

A. Reaction coordinate

DFT calculation results for the reaction coordinate of the initial decomposition paths are summarized in Figure 5 with the DNB molecule shown at zero energy. All energetics are calculated at the B3LYP/6-31++G** level of theory. The details of the geometries for the reactant, intermediate complex, TSs and products are available by request to the corresponding author. Structures of various TSs were optimized using a number of likely high potential energy geometries in reactive trajectories as starting geometries. NO₂ elimination in path 1 is dynamically simple, in that no complicated rearrangement is needed for N-N bond scission. Efforts were made to locate the transition state connecting DNB to products O₂NNHCONHCONH + NO₂. However, various starting geometries corresponding to a dissociating N-N bond converged, instead, to the DNB structure at B3LYP/6-31++G** and MP2/cc-pVDZ levels of theory. We also performed a relaxed potential energy scan running along the dissociating N-N bond using the MP2/cc-pVDZ method. The N-N bond length (r_{NN}) was continuously varied from 1.4 to 3.1 Å, and all coordinates other than r_{NN} were optimized at each point. The asymptotic energy of the resulting PES scan is nearly equal to product energy of O₂NNHCONHCONH + NO₂, suggesting there is no substantial reverse barrier associated with decomposition to O₂NNHCONHCONH + NO₂. It is therefore expected that NO₂ elimination opens at the thermodynamic threshold energy of 1.73 eV and to be facile. Note that previous ab initio calculations using G2 and QCISD(T)//MP2/6-311G** methods indicate that H₂N-NO₂ may dissociate to NH₂ and NO₂ without a reverse barrier, 42,43 and our calculations are consistent with that finding.

The only low energy route for path 2 located computationally appears to be DNB \rightarrow TS_21 \rightarrow O₂NNHCONCO + HNNO₂H. The reaction is endothermic by 0.99 eV; however, the decomposition path bears an energy barrier of 1.16 eV with respect to DNB. Path 3 is slightly more convoluted: DNB \rightarrow

TS_31 \rightarrow twisted DNB \rightarrow TS_32 \rightarrow O₂NNHCONCO + H₂NNO₂, i.e., twisting the nearly planar DNB molecule via an activation barrier TS_31 (0.34 eV above DNB), followed by intra-molecular H-atom transfer and elimination of H₂NNO₂ via the second activation barrier TS_32 (2.13 eV above DNB). One issue for interpretation of paths 2 and 3 products is that HNNO₂H might isomerize to H₂NNO₂, which could affect the subsequent decomposition products. The TS_22 for this isomerization is 1.18 eV above the HNNO₂H energy. It is certainly possible that inter-conversion might occur during the decomposition at detonation temperature. No other low energy pathways were found leading to decomposition paths 1, 2 and 3, although we cannot exclude the possibility that such pathways exist.

2. RRKM results

To evaluate whether the initial decomposition paths identified in trajectory simulations can account for realistic situations, the RRKM program was used to calculate the rates for each individual path at different temperatures. To calculate the RRKM unimolecular rates, sets of vibrational frequencies and rotational constants appropriate for the reactant and the transition states leading to dissociation are required. These are derived from the frequencies and rotational constants calculated at B3LYP/6- $31++G^{**}$, with the frequencies scaled by a factor of 0.955 as suggested by recent work. The rotation quantum number K was treated as active in evaluating the rates k (E, J) so that all (2J+1) K-levels are counted, 44 i.e.,

$$k(E,J) = \frac{d}{h} \frac{\sum_{K=-J}^{J} G[E - E_0 - E_r^{\dagger}(J,K)]}{\sum_{K=-J}^{J} N[E - E_r(J,K)]}$$

where d is the reaction path degeneracy, G is the transition state sum of states, N is the reactant density of states, E_0 is the unimolecular dissociation threshold, and E_r and E_r^{\dagger} are the rotational energies for the reactant and the transition state, respectively.

Since no reverse activation barrier is located for decomposition of DNB to $O_2NNHCONHCONH + NO_2$, vibrational frequencies appropriate to the transition state for NO_2 elimination, hereafter termed TS_1, have to be assumed for the RRKM calculation of path 1 decomposition rates. Two limiting sets of vibrational frequencies have been chosen for TS_1. $^{45-49}$ At one extreme, the vibrational frequencies of

TS 1 are equal to those of DNB with removal of only one mode that corresponds to the reaction coordinate (i.e., the stretching mode of the dissociating N-N bond). As long as there is no reverse activation barrier for decomposition of DNB to O₂NNHCONHCONH and NO₂, this choice reflects the "tightest" TS that is possible, and would provide lower limits to the unimolecular rates for path 1. At the other extreme, a TS estimate was made which consists of 33 frequencies of O₂NNHCONHCONH, 3 frequencies of NO₂, and 5 transitional frequencies. The frequencies of the six transitional modes lost upon dissociation are chosen from DNB. One N-N stretching frequency is chosen as the reaction coordinate and removed. The five remaining transitional frequencies (corresponding to rotations, bends and torsions), which become rotations and translations of completely dissociated products, are scaled by a factor of 0.5 to reflect the looseness of the transition state which changes the entropy of activation (i.e. the difference in entropy between the reactant and the TS). The choice of our scaling factor is empirical and was based on other's work. A similar scaling factor was used by Armentrout's group to assign the transitional modes in dissociation of energized metal ion-ligand complex ML_x. ⁴⁵⁻⁴⁷ Dissociations of these ML_x complexes have no reverse activation barriers, and the ion-induced dipole and ion-dipole forces result in long range metal ligand interactions. Therefore, the corresponding TSs must be truly "loose" TSs. The fact that the similarly scaled translational frequencies were successfully used to extract dissociation energies of ML_x by Armentrout et al., 45-47 suggests that this scaling factor yields appropriate "loose" TSs corresponding to weak associations of the products. In the present work, we employed "tight" and "loose" TS_1, respectively, in two sets of RRKM calculations for path 1 NO2 elimination. The tightness of the transition state significantly affects the reaction rate and thus the branching ratio, and the resulting two sets of RRKM rates provide an estimate of the range of path 1 decomposition rates.

Table IV summarized the RRKM results, including the densities of states (DOS) for the equilibrium and twisted DNB structures, unimolecular rates and decomposition branching ratios. In the Table, k_1 , k_2 , k_{31} represent the rates for crossing TS_1, TS_21, TS_31 leading from the equilibrium DNB structure, while k_{-31} and k_{32} are the rates for crossing TS_31 and TS_32 from the twisted DNB structure,

respectively. The table lists two values for k_1 at each temperature (one in parentheses), which were obtained using "tight" and "loose" TS_1, respectively. According to the values of k_{31} and $k_{.31}$, the interconversion between equilibrium and twisted structures of DNB occurs on a time scale of psec, which is significantly shorter compared to decomposition time scale. Therefore, the relative ratio of equilibrium and twisted DNB structures could be estimated using DOS in these structures. As indicated in Table 4, the values of DOS are temperature dependent. Because the energy of the twisted structure increases by only 0.26 eV compared to the equilibrium one, the DOS ratios for equilibrium:twisted structure are nearly 1:1 from 750K to 2000 K. Consequently, at this temperature range, DNB is best considered to be a mix of two different structures, and the average lifetime of DNB is around 10^{-6} s at 1000 K, decreasing to 10^{-9} s at 1500 K. Under this circumstance, the branching for DNB decomposition can be estimated by the ratio of k_1 , k_2 and k_{32} .

RRKM calculations predict that, at temperatures below 1500 K, path 1 (NO₂ elimination) and path 3 (nitramide elimination) are negligible due to the high and/or tight transition states, and only path 2 (elimination of HNNO₂H) would be expected. Paths 1 and 3 begin to emerge at 1500 K (i.e., the typical denotation temperature⁴⁰), and become significant at high temperature. Depending on the nature of the transition state adopted for the calculations, path 1 may account for 1 - 9% of initial decomposition at 1750 K and 2 - 18% at 2000 K. For the reason discussed above, this branching includes contributions from paths 4, 5 and 6 in addition to path 1. The branching ratio of path 3 is estimated to be 1% at 1500 K, increasing to 5% at 1750 K and 12 - 15% at 2000 K. Since TS_32 (for the formation of nitramide from twisted DNB) and TS_22 (for the formation of nitramide from isomerization of HNNO₂H) have a similar barrier height, it is anticipated that H₂NNO₂ may be produced via both routes above 1500K.

V. Conclusions

Quasi-classical, direct dynamics trajectories for thermal decomposition of DNB were analyzed to probe the decomposition mechanisms and dynamics. The trajectories, calculated at the B3LYP/6-31G* level of theory, are able to reproduce the DNB decomposition products observed in pyrolysis experiments and reveal various decomposition paths leading to these products. RRKM theory was used to verify the

significance of these decomposition paths and calculate the branching ratios at real detonation temperatures, based on the reaction coordinate constructed using trajectory results. According to RRKM analysis, elimination of HNNO₂H, H₂NNO₂ and NO₂, can be important at typical detonation temperatures. While HNNO₂H elimination clearly dominates at the temperature range of 750 - 2000 K, the contributions of other two paths increase substantially with increasing temperature. At 2000K, elimination of nitramide can account for more than 12% of DNB decomposition. Contribution of NO₂ elimination depends on the "tightness" of the associated transition state, and would account for up to 18% of DNB decomposition should the reaction occur via a "loose" transition state. By combining direct dynamics simulations and statistical modeling, we are able to acertain the nature of the reaction mechanisms involved in the initial decomposition of DNB. This work demonstrates the utility of direct dynamics trajectory simulations as a powerful guide for investigating decomposition mechanisms and dynamics of complex energetic molecules, locating transition states for many-atom systems, and constructing the appropriate kinetics model; subsequently, it is necessary to use RRKM or other statistical theories to get meaningful results as far as for the branching ratios at experimental temperatures are concerned.

Acknowledgements

This work was supported by the Air Force Research Laboratory (CUNY Research Foundation Contract no. 16348 with ERC, Inc, Edwards AFB) via AFOSR Contract No. FA9300-06-C-0023. J. Liu would like to thank Scott Anderson (University of Utah) for providing part of computational time and for many stimulating discussions, and Bill Hase (Texas Tech) for providing the VENUS program.

Supporting Information Available:

Video (mpg files) showing representative trajectories.

References

- (1) Geith, J.; Holl, G.; Klapötke, T. M.; Weigand, J. J. Combustion and Flame 2004, 139, 358.
- (2) Geith, J.; Klapöetke, T. M.; Weigand, J.; Holl, G. *Propellants, Explosives, Pyrotechnics* **2004**, 29, 3.
 - (3) Klapöetke, T. M. Structure and Bonding 2007, 125, 85.
- (4) Chambreau, S. D.; Schneider, S.; Rosander, M.; Hawkins, T.; Gallegos, C. J.; Pastewait, M. F.; Vaghjiani, G. L. J. Phys. Chem. A 2008, 112, 7816.
 - (5) Thiele, J.; Uhlfelder, E. Justus Liebigs Ann. Chem. 1898, 303, 93.
 - (6) Köhler, J.; Meyer, R. Explosivstoffe, 9th ed.; VCH: Weinheim, 1998.
- (7) Schneider, S.; Hawkins, T.; Rosander, M.; Vaghjiani, G.; Chambreau, S.; Drake, G. *Energy & Fules* **2008**, 22, 2871.
 - (8) Liu, J.; Anderson, S. L. Int. J. Mass Spectrom. 2005, 241, 173.
 - (9) Wang, I. S. Y.; Karplus, M. J. Am. Chem. Soc. 1973, 95, 8160.
 - (10) Leforestier, C. J. Chem. Phys. 1978, 68, 4406.
 - (11) Car, R.; Parrinello, M. Phys. Rev. Lett. **1985**, 55, 2471.
 - (12) Baldridge, K. K.; Gordon, M. S.; Steckler, R.; Truhlar, D. G. J. Phys. Chem. 1989, 93, 5107.
 - (13) Helgaker, T.; Uggerud, E.; Jensen, H. J. A. Chem. Phys. Lett. 1990, 173, 145.
- (14) Bolton, K.; Hase, W. L. Modern Methods for Multidimensional Dynamics Computations in Chemistry 1998, 143.
- (15) Advances in Classical Trajectory Methods, Vol. 1: Intramolecular and Nonlinear Dynamics; Hase, W. L., Ed.; JAI: Greenwich, 1998.
 - (16) Sun, L.; Song, K.; Hase, W. L. Science 2002, 296, 875.
 - (17) Bakken, V.; Millam, J. M.; Schlegel, H. B. J. Chem. Phys. **1999**, 111, 8773.
 - (18) Marcus, R. A. J. Chem. Phys. 1952, 20, 359.
- (19) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Scalmani, G.; Barone, V.; Mennucci, B.; Petersson, G. A.; Nakatsuji, H.; Caricato, M.; Li, X.; Hratchian, H. P.; Izmaylov, A. F.; Bloino, J.; Zheng, G.; Sonnenberg, J. L.; Hada, M.; Ehara, M.; Toyota, K.; Fukuda, R.; Hasegawa, J.; Ishida, M.; Nakajima, T.; Honda, Y.; Kitao, O.; Nakai, H.; Vreven, T.; J. A. Montgomery, J.; Peralta, J. E.; Ogliaro, F.; Bearpark, M.; Heyd, J. J.; Brothers, E.; Kudin, K. N.; Staroverov, V. N.; Keith, T.; Kobayashi, R.; Normand, J.; Raghavachari, K.; Rendell, A.; Burant, J. C.; Iyengar, S. S.; Tomasi, J.; Cossi, M.; Rega, N.; Millam, J. M.; Klene, M.; Knox, J. E.; Cross, J. B.; Bakken, V.; Adamo, C.; Jaramillo, J.; Gomperts, R.; Stratmann, R. E.; Yazyev, O.; Austin, A. J.; Cammi, R.; Pomelli, C.; Ochterski, J. W.; Martin, R. L.; Morokuma, K.; Zakrzewski, V. G.; Voth, G. A.;

- Salvador, P.; Dannenberg, J. J.; Dapprich, S.; Daniels, A. D.; Farkas, O.; Foresman, J. B.; Ortiz, J. V.; Cioslowski, J.; Fox, D. J. Gaussian 09, Revision B. 01; Gaussian, Inc.: Wallingford CT, 2009.
- (20) Zheng, J.; Alecu, I. M.; Lynch, B. J.; Zhao, Y.; Truhlar, D. G. Database of Frequency Scale Factors for Electronic Model Chemistries, Version 2; http://comp.chem.umn.edu/freqscale/version2.htm, 2010.
- (21) Baer, T.; Hase, W. L. *Unimolecular Reaction Dynamics: Theory and Experiments*; Oxford University Press: New York, 1996.
 - (22) Hase, W. L. Acc. Chem. Res. 1998, 31, 659.
 - (23) Fukui, K. J. Phys. Chem. 1970, 74, 461.
- (24) Zhu, L.; Hase, W. L. A General RRKM Program(QCPE 644), Quantum Chemistry Program Exchange; Chemistry Department, University of Indiana: Bloomington, 1993.
 - (25) Ishikawa, Y.; McQuaid, M. J. J Mol Structure: Theochem 2007, 818, 119.
 - (26) Boyle, J. M.; Uselman, B. w.; Liu, J.; Anderson, S. L. J. Chem. Phys. 2008, 128, 114304.
 - (27) Fang, Y.; Liu, J. J. Phys. Chem. A 2009, 113, 11250.
- (28) Hase, W. L.; Bolton, K.; de Sainte Claire, P.; Duchovic, R. J.; Hu, X.; Komornicki, A.; Li, G.; Lim, K.; Lu, D.; Peslherbe, G. H.; Song, K.; Swamy, K. N.; Vande Linde, S. R.; Varandas, A.; Wang, H.; Wolf, R. J. VENUS99: A general chemical dynamics computer program; Texas Tech University Lubbock, TX, 1999.
 - (29) Bacskay, G. B. Chem. Phys. 1981, 61, 385.
- (30) Lias, S. G. Ionization Energy Evaluation. In *NIST Standard Reference Database Number 69*; Linstrom, P. J., Mallard, W. G., Eds.; National Institute of Standards and Technology: Gaithersburg, MD, 2003; pp http://webbook.nist.gov.
- (31) Laaksonen, L. gOpenMol; 3.0 ed.; Center for Scientific Computing. : Espoo, Finland, 2005; pp available at www.csc.fi/gopenmol/.
 - (32) Liu, J.; Song, K.; Hase, W. L.; Anderson, S. L. J. Phys. Chem. A 2005, 109, 11376.
 - (33) Liu, J.; Song, K.; Hase, W. L.; Anderson, S. L. J. Am. Chem. Soc. 2004, 126, 8602.
 - (34) Liu, J.; Song, K.; Hase, W. L.; Anderson, S. L. J. Chem. Phys. 2003, 119, 3040.
 - (35) Liu, J.; Uselman, B.; Boyle, J.; Anderson, S. L. J. Chem. Phys. **2006**, 125, 133115.
 - (36) Liu, J.; Anderson, S. L. Phys. Chem. Chem. Phys. 2009, 11, 8721.
 - (37) Fang, Y.; Liu, F.; Bennett, A.; Ara, S.; Liu, J. J. Phys. Chem. B **2011**, 115, 2671.
 - (38) Untch, A.; Schinke, R.; Cotting, R.; Huber, J. R. J. Chem. Phys. 1993, 99, 9553.
 - (39) Miller, W. H.; Hase, W. L.; Darling, C. L. J. Chem. Phys. 1989, 91, 2863.
 - (40) Chambreau, S. personal communication **2010**.
 - (41) Herath, N.; Suits, A. G. J. Phys. Chem. Lett. **2010**, 2, 642.

- (42) Seminario, J. M.; Politzer, P. Int. J. Quantum. Chem.: Quantum Chemistry Symposium 1992, 26, 497.
 - (43) Mebel, A. M.; Hsu, C.-C.; Lin, M. C.; Morokuma, K. J. Chem. Phys. 1995, 103, 5640.
 - (44) Zhu, L.; Hase, W. L. Chem. Phys. Lett. 1990, 175, 117.
 - (45) Meyer, F.; Khan, F. A.; Armentrout, P. B. J. Am. Chem. Soc. 1995, 117, 9740.
- (46) More, M. B.; Glendening, E. D.; Ray, D.; Feller, D.; Armentrout, P. B. *J. Phys. Chem.* **1996**, 100, 1605.
- (47) Ray, D.; Feller, D.; More, M. B.; Glendening, E. D.; Armentrout, P. B. *J. Phys. Chem.* **1996**, *100*, 16116.
 - (48) Rodgers, M. T.; Armentrout, P. B. J. Chem. Phys. 1998, 109, 1787.
 - (49) Rodgers, M. T.; Ervin, K. M.; Armentrout, P. B. J. Chem. Phys. 1997, 106, 4499.
 - (50) Liu, J.; Devener, B. V.; Anderson, S. L. J. Chem. Phys. 2002, 117, 8292.

 $\textbf{Table 1.} \hspace{0.5cm} \text{Calculated enthalpy of detonation } (\Delta_r H) \text{ of DNB } (kJ/mol)$

Methods	B3LYP/6-31G	B3LYP/6-31G*	B3LYP/6-31+G*	B3LYP/6-31++G**	MP2/cc-pVTZ ^a
$\Delta_{\rm r}H$	-606	-695	-739	-757	-863

^a Ref 2

 Table 2.
 Calculated DNB vibrational and rotational energies at various temperatures

T / K	298	500	750	1000	1250	1500	1750	2000	4000	5000	6000
E _{vib} / eV	0.26	0.65	1.27	1.99	2.76	3.57	4.40	5.24	12.25	15.82	19.41
E_{rot}/eV	0.04	0.06	0.10	0.13	0.16	0.19	0.23	0.26	0.52	0.65	0.78

 Table 3.
 Direct dynamics trajectory simulation results of DNB decomposition

		ΔH^{a}	Branching ratio % ^b			
Path	Decomposition products	/eV	4000K	5000K	6000K	
1*		1.73	34	39	43	
	O N H C x2 H O O	2.43				
	* some trajectories dissociate to NO ₂ , HN ₂ O ₂ and HNCO simultaneously					
2		0.99	26	13	7	
		-0.93				
3		0.26	10	6	4	
		0.54				
4		1.73	4	8	10	
		0.80				
		1.11				

 Table 3. (Continued)

D 4		ΔH ^a /eV	Bran	ching ratio) % ^b
Path	Decomposition products		4000K	5000K	6000K
5		1.73	8	13	26
	O H O N O H O N O H O N O H O N O H O N O N O H O N O N O N O N O N O N O N O N O N O N	3.02			
6	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1.81	0	5	0
	O H H NO H NO H NO	0.98			
	Sum of other dissociation paths	0	8	16	10
	Non-reactive	0	10	0	0

 $^{^{}a}$ Values of ΔH were calculated relative to DNB, at the B3LYP/6-31++G** level of theory.

b Branching ratios were calculated based on 50 trajectories at each temperature.

 Table 4.
 RRKM results for initial decomposition of DNB

Temp / K	750	1000	1250	1500	1750	2000
		d	ensity of states (1/cm ⁻¹)		
DNB	1.95×10^{18}	2.34×10^{22}	5.98×10^{25}	4.94×10^{28}	1.71×10^{31}	2.92×10^{33}
twisted DNB	1.90×10^{18}	2.33×10^{22}	6.04×10^{25}	5.04×10^{28}	1.75×10^{31}	3.02×10^{33}
		uı	nimolecular rates	$(s^{-1})^a$		
k_I	0 (0)	0.6 (3.6)	$1.8 \times 10^4 \\ (1.8 \times 10^5)$	2.1×10^6 (2.7×10^7)	3.9×10^7 (5.8×10^8)	$2.9 \times 10^{8} $ (4.7×10^{9})
k_2	8.5	9.7×10^{5}	7.9×10^{7}	1.0×10^{9}	5.5×10^{9}	1.8×10^{10}
k_{31}	3.4×10^{9}	1.5×10^{10}	3.5×10^{10}	6.0×10^{10}	8.8×10^{10}	1.2×10^{11}
k ₋₃₁	2.4×10^{11}	3.2×10^{11}	3.8×10^{11}	4.4×10^{11}	4.8×10^{11}	5.1×10^{11}
k_{32}	0	1.5×10^{-2}	2.1×10^{4}	7.9×10^{6}	2.9×10^{8}	3.4×10^{9}
		1	oranching ratios ((%) ^a		
path 1	0	0	0 (0.3)	0.2 (2.6)	0.7 (9.1)	1.3 (18.0)
path 2	100	100	100 (99.7)	99.0 (96.7)	94.3 (86.3)	83.3 (69.2)
path 3	0	0	0	0.8 (0.8)	5.0 (4.5)	15.4 (12.8)

 k_1 , k_2 , k_{31} are the rate constants for crossing TS_1, TS_21, TS_31 from DNB, and k_{-31} and k_{32} are the rate constants for crossing TS_31 and TS_32 from twisted DNB, respectively. The k_1 values in parentheses were obtained using a "loose" TS_1.

Figure Captions

- Figure 1 B3LYP/6-31++G** optimized structures of DNB and products identified in trajectories.
- Figure 2 A representative trajectory of decomposition path 1, simulated at 4000 K using the B3LYP/6-31G* method. Plot shows variation of potential energy during the trajectory, and the snap shots show three sequential elimination steps.
- Figure 3 A representative trajectory of decomposition path 2, simulated at 4000 K using the B3LYP/6-31G* method. Plot shows variation of potential energy during the trajectory, and the snap shots show elimination of HNNO₂H and its subsequent dissociation to N₂O and water.
- Figure 4 A representative trajectory of decomposition path 3, simulated at 4000 K using the B3LYP/6-31G* method. Plot shows variation of potential energy during the trajectory, and the snap shots show elimination of H₂NNO₂ via twisting the molecular plane followed by intramolecular H-atom transfer.
- Figure 5 Schematic reaction coordinate for the initial decomposition of DNB. Energetics of complexes, TSs, and products are derived from B3LYP/6-31++G** calculations, including ZPE. For TSs, vibrational modes corresponding to the imaginary frequencies are indicated by displacement vectors.

Fig. 1

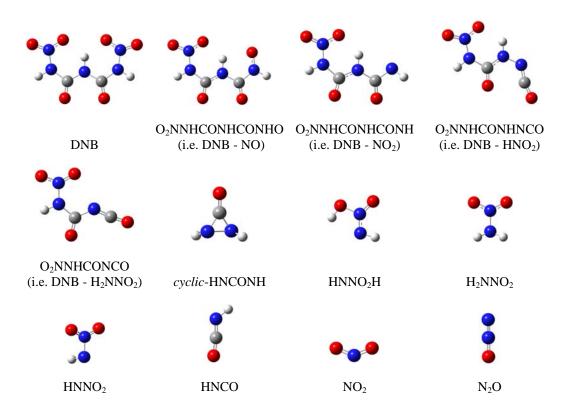


Fig. 2

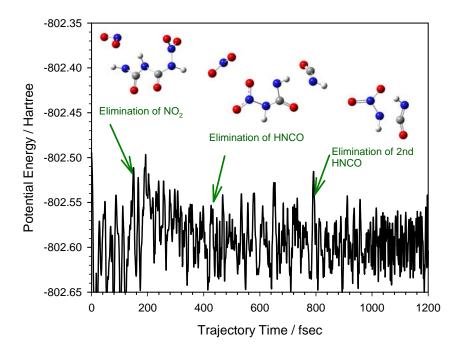


Fig. 3

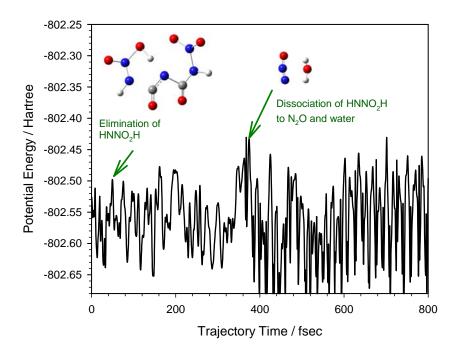


Fig .4

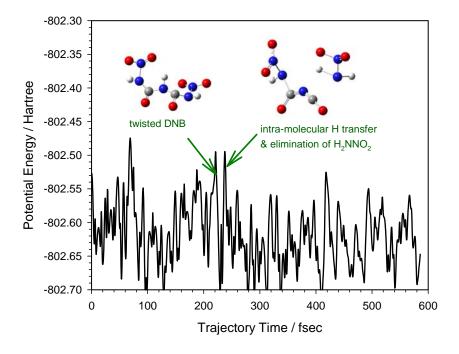


Fig. 5

